## MATH 205: Statistical methods

Lab 7: Confidence intervals

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## A good prediction comes with a range



MATH 205: Statistical methods

- Assume that you have been using an AI to predict the stock price of Microsoft every day in the last few years
- The prediction comes as a range, e.g., [295, 305]
- The algorithm, on average, is correct 95 out of 100 days
- $\bullet\,$  Then we say that a prediction from this AI has a confidence of  $95\%\,$

## Confidence intervals



95% confidence interval: If we repeat the experiment many times, the interval contains  $\mu$  about 95% of the time

- I generate 100 observations from normal random variable with (true) mean μ and standard deviation 1 (but I don't let you know the value of μ). I then ask you to estimate the μ.
- It is natural to estimate  $\mu$  by a range centered at the sample mean  $\bar{x}$
- The question is: what should the width of this range be?