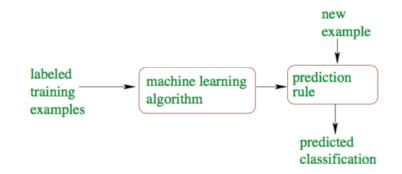
Mathematical techniques in data science

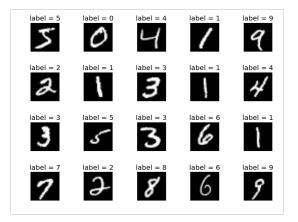
Lecture 3: Nearest neighbors



Learning a function that maps an input to an output based on example input-output pairs

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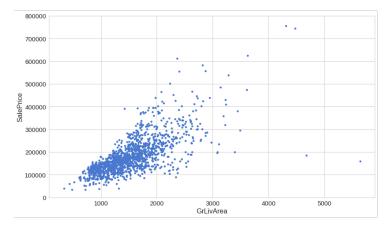
Hand-written digit recognition



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Predict house price by living area



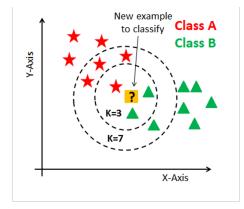
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- Very simple idea: Make predictions based on labels of the nearest training examples
- Applicable to both classification and regression

K-nearest neighbor (K-NN) for classification

- Learning: Store all training examples
- Predict label of x:
 - Find the nearest K training examples to x
 - Assign the most frequent label to x

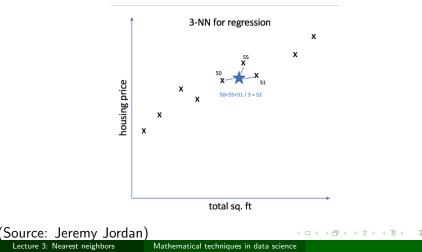


(Source: kdnuggets.com)

Lecture 3: Nearest neighbors

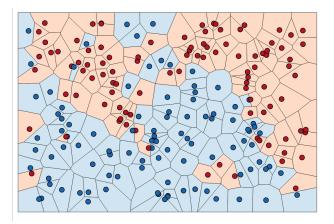
K-nearest neighbor (K-NN) for regression

- Learning: Store all training examples
- Predict label of x:
 - Find the nearest K training examples to x
 - Assign the average of the K nearest labels to x



Decision boundary for K-NN (classification)

- Divide feature space into Voronoi cells
- Decision boundaries are linear



(Source: Kevin Zakka)

Lecture 3: Nearest neighbors

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- Need to define a distance metric between data points
- Common metric: Euclidean distance (L2 distance)

$$d(x, x') = \sqrt{\sum_{i=1}^{n} (x_i - x'_i)^2}$$

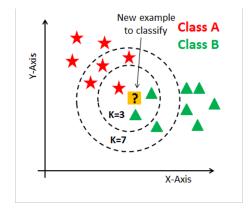
• Other metrics: Manhattan distance, Minkowski distance, etc.

• Simplest algorithm: brute-force search

- Compute distance between every training data point to the test point
- Pick K points with the smallest distances
- Space partitioning algorithms: arrange data points into some data structure (such as a binary tree) for faster search
 - Ball tree (https://en.wikipedia.org/wiki/Ball_tree)
 - k-d tree (https://en.wikipedia.org/wiki/K-d_tree)
- Approximate algorithms

Variant: Prediction with non-uniform weights

Nearer neighbors have more weights when making predictions



Keys to read the documentations

- Parameters (to set up the model)
- Methods (what we can do with the model)
- Attributes (components we can extract from the model)

Nearest Neighbors on scikit-learn

sklearn.neighbors.KNeighborsClassifier

class sklearn.neighbors. KNeighborsClassifier(n_neighbors=5, *, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n_jobs=None, **kwargs) [source]

Classifier implementing the k-nearest neighbors vote.

Read more in the User Guide.

Parameters:	n_neighbors : <i>int, default=5</i> Number of neighbors to use by default for kneighbors queries.
	weights : {'uniform', 'distance'} or callable, default='uniform'
	weight function used in prediction. Possible values:
	'uniform' : uniform weights. All points in each neighborhood are weighted equally.
	'distance': weight points by the inverse of their distance. in this case, closer neighbors of a query
	point will have a greater influence than neighbors which are further away.
	 [callable] : a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.
	algorithm : {'auto', 'ball_tree', 'kd_tree', 'brute'}, default='auto'
	Algorithm used to compute the nearest neighbors:
	'ball_tree' will use BallTree
	 'kd_tree' will use KDT ree
	 'brute' will use a brute-force search.
	 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Nearest Neighbors on scikit-learn

	sklearn.neighbors.KNeighborsRegressor			
	eighbors. KNeighborsRegressor(n_neighbors=5, *, weights='uniform', algorithm='auto', leaf_size=30, nkowski', metric_params=None, n_jobs=None, **kwargs) ¶ [source			
Regression base	ed on k-nearest neighbors.			
The target is predicted by local interpolation of the targets associated of the nearest neighbors in the training set.				
Read more in the User Guide.				
New in version (0.9.			
Parameters: n neighbors : int, default=5				
i didinetero.	Number of neighbors to use by default for kneighbors queries.			
	weights : {'uniform', 'distance'} or callable, default='uniform' weight function used in prediction. Possible values:			
	 'uniform': uniform weights. All points in each neighborhood are weighted equally. 'distance': weight points by the inverse of their distance. in this case, closer neighbors of a quer point will have a greater influence than neighbors which are further away. [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights. 			
	Uniform weights are used by default.			
	algorithm : {'auto', 'ball_tree', 'kd_tree', 'brute'), default='auto' Algorithm used to compute the nearest neighbors:			
	'ball_tree' will use BallTree			
	 'kd_tree' will use KDTree 'brute' will use a brute-force search. 			
	 'brute' will use a brute-torce search. 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit 			

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Nearest Neighbors on scikit-learn

sklearn.neighbors: Nearest Neighbors

The sklearn.neighbors module implements the k-nearest neighbors algorithm.

User guide: See the Nearest Neighbors section for further details.

<pre>neighbors.BallTree(X[, leaf_size, metric])</pre>	BallTree for fast generalized N-point problems
neighbors.DistanceMetric	DistanceMetric class
<pre>neighbors.KDTree(X[, leaf_size, metric])</pre>	KDTree for fast generalized N-point problems
<pre>neighbors.KernelDensity(*[, bandwidth,])</pre>	Kernel Density Estimation.
<pre>neighbors.KNeighborsClassifier([])</pre>	Classifier implementing the k-nearest neighbors vote.
<pre>neighbors.KNeighborsRegressor([n_neighbors,])</pre>	Regression based on k-nearest neighbors.
<pre>neighbors.KNeighborsTransformer(*[, mode,])</pre>	Transform X into a (weighted) graph of k nearest neighbors
<pre>neighbors.LocalOutlierFactor([n_neighbors,])</pre>	Unsupervised Outlier Detection using Local Outlier Factor (LOF)
<pre>neighbors.RadiusNeighborsClassifier([])</pre>	Classifier implementing a vote among neighbors within a given radius
neighbors.RadiusNeighborsRegressor([radius,])	Regression based on neighbors within a fixed radius.
<pre>neighbors.RadiusNeighborsTransformer(*[,])</pre>	Transform X into a (weighted) graph of neighbors nearer than a radius
<pre>neighbors.NearestCentroid([metric,])</pre>	Nearest centroid classifier.
<pre>neighbors.NearestNeighbors(*[, n_neighbors,])</pre>	Unsupervised learner for implementing neighbor searches.
<pre>neighbors.NeighborhoodComponentsAnalysis([])</pre>	Neighborhood Components Analysis

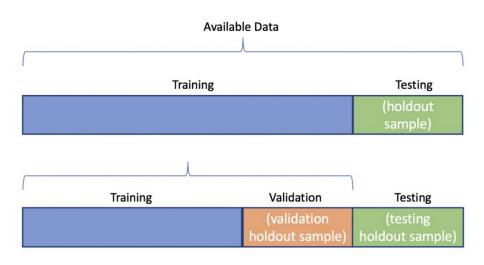
neighbors.kneighbors_graph(X, n_neighbors, *) Computes the (weighted) graph of k-Neighbors for points in X neighbors.radius_neighbors_graph(X, radius, *) Computes the (weighted) graph of Neighbors for points in X

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- Get and pre-process data
- Visualize the data (optional)
- Create a model
- Train the model; i.e. call model.fit()
- Predict on test data
- Compute evaluation metrics (accuracy, mean squared error, etc.)
- Visualize the trained model (optional)

- How effective the model makes predictions on new (unseen) data
- Classification: accuracy or error rate
- Regression: average (squared) distance between predicted and true values (mean squared error)

Review: Data splitting practices



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